

# Vector Algebra

Question 1.

A unit vector perpendicular to the plane of

$\vec{a} = 2\hat{i} - 6\hat{j} - 3\hat{k}$  and  $\vec{b} = 4\hat{i} + 3\hat{j} - \hat{k}$  is

- (a)  $\frac{4\hat{i} + 3\hat{j} - \hat{k}}{\sqrt{26}}$  (b)  $\frac{2\hat{i} - 6\hat{j} - \hat{k}}{7}$   
(c)  $\frac{3\hat{i} - 2\hat{j} + 6\hat{k}}{7}$  (d)  $\frac{2\hat{i} - 3\hat{j} - 6\hat{k}}{7}$

Answer:

- (c)  $\frac{3\hat{i} - 2\hat{j} + 6\hat{k}}{7}$

Question 2.

The area of parallelogram whose adjacent sides are  $\hat{i} - 2\hat{j} + 3\hat{k}$  and  $2\hat{i} + \hat{j} - 4\hat{k}$  is

- (a)  $10\sqrt{6}$   
(b)  $5\sqrt{6}$   
(c)  $10\sqrt{3}$   
(d)  $5\sqrt{3}$

Answer:

- (b)  $5\sqrt{6}$

Question 3.

If  $\vec{AB} \times \vec{AC} = 2\hat{i} - 4\hat{j} + 4\hat{k}$ , then the area of  $\triangle ABC$  is

- (a) 3 sq. units  
(b) 4 sq. units  
(c) 16 sq. units  
(d) 9 sq. units

Answer:

- (a) 3 sq. units

Question 4.

**A vector of magnitude 5 and perpendicular to  $(\hat{i} - 2\hat{j} + \hat{k})$  and  $(2\hat{i} + \hat{j} - 3\hat{k})$  is**

- (a)  $\frac{5\sqrt{3}}{3}(\hat{i} + \hat{j} + \hat{k})$       (b)  $\frac{5\sqrt{3}}{3}(\hat{i} + \hat{j} - \hat{k})$   
(c)  $\frac{5\sqrt{3}}{3}(\hat{i} - \hat{j} + \hat{k})$       (d)  $\frac{5\sqrt{3}}{3}(-\hat{i} + \hat{j} + \hat{k})$

Answer:

(a)  $\frac{5\sqrt{3}}{3}(\hat{i} + \hat{j} + \hat{k})$

Question 5.

$|a \times b|^2 + |a \cdot b|^2 = 144$  and  $|a| = 4$ , then  $|b|$  is equal to

- (a) 12  
(b) 3  
(c) 8  
(d) 4

Answer:

(b) 3

Question 6.

If  $|a \times b| = 4$  and  $|a \cdot b| = 2$ , then  $|a|^2 |b|^2$  is equal to

- (a) 2  
(b) 6  
(c) 8  
(d) 20

Answer:

(d) 20

Question 7.

**If  $\vec{a} = (\hat{i} + \hat{j} + \hat{k})$ ,  $\vec{a} \cdot \vec{b} = 1$  and  $\vec{a} \times \vec{b} = \hat{j} - \hat{k}$ , then  $\vec{b}$  is**

- (a)  $\hat{i} - \hat{j} + \hat{k}$     (b)  $2\hat{j} - \hat{k}$     (c)  $\hat{i}$       (d)  $2\hat{i}$

Answer:

(c)  $\hat{i}$

Question 8.

The two vectors  $a = 2\hat{i} + \hat{j} + 3\hat{k}$  and  $b = 4\hat{i} - \lambda\hat{j} + 6\hat{k}$  are parallel, if  $\lambda$  is equal to

- (a) 2
- (b) -3
- (c) 3
- (d) 2

Answer:

- (d) 2

Question 9.

If  $|a|=5$ ,  $|b|=13$  and  $|a \times b|=25$ , find  $a \cdot b$

- (a)  $\pm 10$
- (b)  $\pm 40$
- (c)  $\pm 60$
- (d)  $\pm 25$

Answer:

- (c)  $\pm 60$

Question 10.

Find the value of  $\lambda$  so that the vectors  $2\hat{i} - 4\hat{j} + \hat{k}$  and  $4\hat{i} - 8\hat{j} + \lambda\hat{k}$  are parallel.

- (a) -1
- (b) 3
- (c) -4
- (d) 2

Answer:

- (d) 2

Question 11.

If O is origin and C is the mid point of A(2, -1) and B(-4, 3), then the value of OC is

- (a)  $\hat{i} + \hat{j}$
- (b)  $\hat{i} - \hat{j}$
- (c)  $-\hat{i} + \hat{j}$
- (d)  $-\hat{i} - \hat{j}$

Answer:

- (c)  $-\hat{i} + \hat{j}$

Question 12.

The vectors  $\vec{AB} = 3\hat{i} + 4\hat{k}$  and  $\vec{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$  are the side of a  $\triangle ABC$ . The length of the median through A is

- (a)  $\sqrt{18}$
- (b)  $\sqrt{72}$
- (c)  $\sqrt{33}$
- (d)  $\sqrt{288}$

Answer:

(c)  $\sqrt{33}$

Question 13.

The summation of two unit vectors is a third unit vector, then the modulus of the difference of the unit vector is

(a)  $\sqrt{3}$

(b)  $1 - \sqrt{3}$

(c)  $1 + \sqrt{3}$

(d)  $-\sqrt{3}$

Answer:

(a)  $\sqrt{3}$

Question 14.

Let  $\vec{a} = \hat{i} + \hat{j} - \hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$  and  $\hat{c}$  be a unit vector perpendicular to  $\vec{a}$  and coplanar with  $\vec{a}$  and  $\vec{b}$ , then  $\hat{c}$  is

(a)  $\frac{1}{\sqrt{2}}(\hat{j} + \hat{k})$

(b)  $\frac{1}{\sqrt{2}}(\hat{j} - \hat{k})$

(c)  $\frac{1}{\sqrt{6}}(\hat{i} - 2\hat{j} + \hat{k})$

(d)  $\frac{1}{\sqrt{6}}(2\hat{i} - \hat{j} + \hat{k})$

Answer:

(d)  $\frac{1}{\sqrt{6}}(2\hat{i} - \hat{j} + \hat{k})$

Question 15.

If  $\vec{a}$  and  $\vec{b}$  are unit vectors enclosing an angle  $\theta$  and  $|\vec{a} + \vec{b}| < 1$ , then

(a)  $\theta = \frac{\pi}{2}$

(b)  $\theta < \frac{\pi}{3}$  (c)

$\pi \geq \theta > \frac{2\pi}{3}$

(d)  $\frac{\pi}{3} < \theta < \frac{2\pi}{3}$

Answer:

(c)  $\pi \geq \theta > \frac{2\pi}{3}$

Question 16.

The value of  $\lambda$  for which the vectors  $3\hat{i} - 6\hat{j} + \hat{k}$  and  $2\hat{i} - 4\hat{j} + \lambda\hat{k}$  are parallel is

- (a)  $\frac{2}{3}$
- (b)  $\frac{3}{2}$
- (c)  $\frac{5}{2}$
- (d)  $\frac{2}{5}$

Answer:

- (a)  $\frac{2}{3}$

Question 17.

The vectors from origin to the points A and B are  $a = 2\hat{i} - 3\hat{j} + 2\hat{k}$  and  $b = 2\hat{i} + 3\hat{j} + \hat{k}$ , respectively then the area of triangle OAB is

- (a) 340
- (b)  $\sqrt{25}$
- (c)  $\sqrt{229}$
- (d)  $\frac{1}{2} \sqrt{229}$

Answer:

- (d)  $\frac{1}{2} \sqrt{229}$

Question 18.

The vectors  $\lambda\hat{i} + \hat{j} + 2\hat{k}$ ,  $\hat{i} + \lambda\hat{j} - \hat{k}$  and  $2\hat{i} - \hat{j} + \lambda\hat{k}$  are coplanar if

- (a)  $\lambda = -2$
- (b)  $\lambda = 0$
- (c)  $\lambda = 1$
- (d)  $\lambda = -1$

Answer:

- (a)  $\lambda = -2$

Question 19.

If  $a, b, c$  are unit vectors such that  $a + b + c = 0$ , then the value of  $a \cdot b + b \cdot c + c \cdot a$  is

- (a) 1
- (b) 3
- (c)  $-\frac{3}{2}$
- (d) None of these

Answer:

- (c)  $-\frac{3}{2}$

Question 20.

If  $|a| = 4$  and  $-3 \leq \lambda \leq 2$ , then the range of  $|\lambda a|$  is

- (a)  $[0, 8]$

- (b)  $[-12, 8]$
- (c)  $[0, 12]$
- (d)  $[8, 12]$

Answer:

- (c)  $[0, 12]$

Question 21.

The number of vectors of unit length perpendicular to the vectors  $a = 2\hat{i} + \hat{j} + 2\hat{k}$  and  $b = \hat{j} + \hat{k}$  is

- (a) one
- (b) two
- (c) three
- (d) infinite

Answer:

- (b) two

Question 22.

Let  $a$ ,  $b$  and  $c$  be vectors with magnitudes 3, 4 and 5 respectively and  $a + b + c = 0$ , then the values of  $a \cdot b + b \cdot c + c \cdot a$  is

- (a) 47
- (b) 25
- (c) 50
- (d) -25

Answer:

- (d) -25

Question 23.

If  $|a| = |b| = 1$  and  $|a + b| = \sqrt{3}$ , then the value of  $(3a - 4b) \cdot (2a + 5b)$  is

- (a) -21
- (b)  $-\frac{21}{2}$
- (c) 21
- (d)  $\frac{21}{2}$

Answer:

- (b)  $-\frac{21}{2}$

Question 24.

The unit vector perpendicular to  $\hat{i} - \hat{j}$  and coplanar with  $\hat{i} + 2\hat{j}$  and  $2\hat{i} + 3\hat{j}$  is

- (a)  $\frac{2\hat{i} - 5\hat{j}}{\sqrt{29}}$  (b)  $2\hat{i} + 5\hat{j}$   
(c)  $\frac{1}{\sqrt{2}}(\hat{i} + \hat{j})$  (d)  $\hat{i} + \hat{j}$

Answer:

- (c)  $\frac{1}{\sqrt{2}}(\hat{i} + \hat{j})$

Question 25.

If  $|a - b| = |a| = |b| = 1$ , then the angle between a and b is

- (a)  $\frac{\pi}{3}$   
(b)  $\frac{3\pi}{4}$   
(c)  $\frac{\pi}{2}$   
(d) 0

Answer:

- (a)  $\frac{\pi}{3}$

Question 26.

$(\vec{a} \cdot \hat{i})^2 + (\vec{a} \cdot \hat{j})^2 + (\vec{a} \cdot \hat{k})^2$  is equal to

- (a) 1 (b)  $\vec{a}$  (c)  $-\vec{a}$  (d)  $|\vec{a}|^2$

Answer:

- (d)  $|\vec{a}|^2$

Question 27.

a, b, c are three vectors, such that  $a + b + c = 0$ ,  $|a| = 1$ ,  $|b| = 2$ ,  $|c| = 3$ , then  $a \cdot b + b \cdot c + c \cdot a$  is equal to

- (a) 0  
(b) -7  
(c) 7  
(d) 1

Answer:

- (b) -7

Question 28.

If  $|a + b| = |a - b|$ , then angle between a and b is ( $a \neq 0$ ,  $b \neq 0$ )

- (a)  $\frac{\pi}{3}$
- (b)  $\frac{\pi}{6}$
- (c)  $\frac{\pi}{4}$
- (d)  $\frac{\pi}{2}$

Answer:

- (d)  $\frac{\pi}{2}$

Question 29.

If  $a$  and  $b$  are two unit vectors inclined to  $x$ -axis at angles  $30^\circ$  and  $120^\circ$  respectively, then  $|a + b|$  equals

- (a)  $\sqrt{\frac{2}{3}}$
- (b)  $\sqrt{2}$
- (c)  $\sqrt{3}$
- (d) 2

Answer:

- (d) 2

Question 30.

If the angle between  $\hat{i} + \hat{k}$  and  $\hat{i} + \hat{j} + a\hat{k}$  is  $\frac{\pi}{3}$ , then the value of  $a$  is

- (a) 0 or 2
- (b) -4 or 0
- (c) 0 or -3
- (d) 2 or -2

Answer:

- (b) -4 or 0

Question 31.

The length of longer diagonal of the parallelogram constructed on  $5a + 2b$  and  $a - 3b$ . If it is given that

$|a| = 2\sqrt{2}$ ,  $|b| = 3$  and angle between  $a$  and  $b$  is  $\frac{\pi}{4}$ , is

- (a) 15
- (b)  $\sqrt{113}$
- (c)  $\sqrt{593}$
- (d)  $\sqrt{369}$

Answer:

- (c)  $\sqrt{593}$

Question 32.

If  $\left(\frac{1}{2}, \frac{1}{3}, n\right)$  are the direction cosines of a line, then the value of  $n$  is

- (a)  $\frac{\sqrt{23}}{6}$



(b)  $\frac{23}{6}$

(c)  $\frac{2}{3}$

(d)  $\frac{3}{2}$

Answer:

(a)  $\frac{\sqrt{23}}{6}$

Question 33.

Find the magnitude of vector  $3\hat{i} + 2\hat{j} + 12\hat{k}$ .

(a)  $\sqrt{157}$

(b)  $4\sqrt{11}$

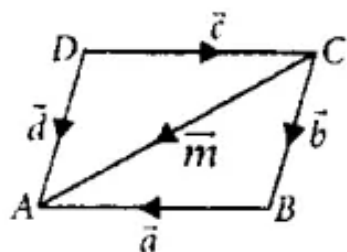
(c)  $\sqrt{213}$

(d)  $9\sqrt{3}$

Answer:

(a)  $\sqrt{157}$

Direction (34 – 36): Study the given parallelogram and answer the following questions.



Question 34.

Which of the following represents equal vectors?

(a) a, c

(b) b, d

(c) b, c

(d) m, d

Answer:

(b) b, d

Question 35.

Which of the following represents collinear but not equal vectors?

(a) a, c

(b) b, d

(c) b, m

(d) Both (a) and (b)

Answer:

(a) a, c

Question 36.

Which of the following represents coinital vector?

- (a) c, d
- (b) m, b
- (c) b, d
- (d) Both (a) and (b)

Answer:

- (d) Both (a) and (b)

Question 37.

The unit vector in the direction of the sum of vectors

$\hat{i} + \hat{j} + \hat{k}$  and  $2\hat{i} + 3\hat{j} + 4\hat{k}$  is

- (a)  $\frac{1}{5\sqrt{2}}(3\hat{i} + 4\hat{j} + 5\hat{k})$
- (b)  $\frac{1}{5\sqrt{2}}(3\hat{i} - 4\hat{j} - 5\hat{k})$
- (c)  $\frac{1}{2\sqrt{2}}(4\hat{i} + 3\hat{j} + 5\hat{k})$
- (d)  $\frac{1}{3\sqrt{2}}(-3\hat{k} + 4\hat{i} + 5\hat{j})$

Answer:

- (a)  $\frac{1}{5\sqrt{2}}(3\hat{i} + 4\hat{j} + 5\hat{k})$

Question 38.

The vectors  $3\hat{i} + 5\hat{j} + 2\hat{k}$ ,  $2\hat{i} - 3\hat{j} - 5\hat{k}$  and  $5\hat{i} + 2\hat{j} - 3\hat{k}$  form the sides of

- (a) Isosceles triangle
- (b) Right triangle
- (c) Scalene triangle
- (d) Equilateral triangle

Answer:

- (d) Equilateral triangle

Question 39.

If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = 4\hat{i} + 3\hat{j} + 4\hat{k}$  and  $\vec{c} = \hat{i} + \alpha\hat{j} + \beta\hat{k}$  are

linearly dependent vectors and  $|\vec{c}| = \sqrt{3}$ , then

- (a)  $\alpha = 1, \beta = -1$
- (b)  $\alpha = 1, \beta = \pm 1$
- (c)  $\alpha = -1, \beta = \pm 1$
- (d)  $\alpha = \pm 1, \beta = 1$

Answer:

- (d)  $\alpha = \pm 1, \beta = 1$

Question 40.

The vectors  $a = x\hat{i} - 2\hat{j} + 5\hat{k}$  and  $b = \hat{i} + y\hat{j} - z\hat{k}$  are collinear, if

- (a)  $x=1, y=-2, z=-5$
- (b)  $x=1.2, y=-4, z=-10$
- (c)  $x=-1/2, y=4, z=10$
- (d) All of these

Answer:

- (d) All of these

Question 41.

The vector  $\hat{i} + x\hat{j} + 3\hat{k}$  is rotated through an angle  $\theta$  and doubled in magnitude, then it becomes  $4\hat{i} + (4x - 2)\hat{i} + 2\hat{k}$ . The value of  $x$  is

- (a)  $\left\{-\frac{2}{3}, 2\right\}$
- (b)  $\left\{\frac{1}{3}, 2\right\}$
- (c)  $\left\{\frac{2}{3}, 0\right\}$
- (d)  $\{2, 7\}$

Answer:

- (a)  $\left\{-\frac{2}{3}, 2\right\}$

Question 42.

If  $a + b + c = 0$ , then  $a \times b =$

- (a)  $c \times a$
- (b)  $b \times c$
- (c) 0
- (d) Both (a) and (b)

Answer:

- (d) Both (a) and (b)

Question 43.

If  $a$  is perpendicular to  $b$  and  $c$ ,  $|a| = 2$ ,  $|b| = 3$ ,  $|c| = 4$  and the angle between  $b$  and  $c$  is  $\frac{2\pi}{3}$ ,  $|abc|$  is equal to

- (a)  $4\sqrt{3}$
- (b)  $6\sqrt{3}$
- (c)  $12\sqrt{3}$
- (d)  $18\sqrt{3}$

Answer:

- (c)  $12\sqrt{3}$

Question 44.

If  $\vec{b}$  and  $\vec{c}$  are any two non-collinear unit vectors and  $\vec{a}$  is any vector, then

$(\vec{a} \cdot \vec{b})\vec{b} + (\vec{a} \cdot \vec{c})\vec{c} + \frac{\vec{a} \cdot (\vec{b} \times \vec{c})}{|\vec{b} \times \vec{c}|} (\vec{b} \times \vec{c})$  is equal to

- (a)  $\vec{0}$       (b)  $\vec{a}$       (c)  $\vec{b}$       (d)  $\vec{c}$

Answer:

(b) a

Question 45.

Let  $\vec{a} = \hat{i} - \hat{k}$ ,  $\vec{b} = x\hat{i} + \hat{j} + (1-x)\hat{k}$  and

$\vec{c} = y\hat{i} + x\hat{j} + (1+x-y)\hat{k}$ . Then,  $[\vec{a} \vec{b} \vec{c}]$  depends on

- (a) neither  $x$  nor  $y$       (b) both  $x$  and  $y$   
(c) only  $x$       (d) only  $y$

Answer:

(a) neither  $x$  nor  $y$

Question 46.

If  $a, b, c$  are three non-coplanar vectors, then  $(a + b + c) \cdot [(a + b) \times (a + c)]$  is

- (a) 0  
(b)  $2[abc]$   
(c)  $-[abc]$   
(d)  $[abc]$

Answer:

(c)  $-[abc]$

Question 47.

If  $u, v$  and  $w$  are three non-coplanar vectors, then  $(u + v - w) \cdot [(u - v) \times (v - w)]$  equals

- (a) 0  
(b)  $u \cdot v \times w$   
(c)  $u \cdot w \times v$   
(d)  $3u \cdot v \times w$

Answer:

(b)  $u \cdot v \times w$

Question 48.

If unit vector  $c$  makes an angle  $\frac{\pi}{3}$  with  $\hat{i} \times \hat{j}$ , then minimum and maximum values of  $(\hat{i} \times \hat{j}) \cdot c$

respectively are

- (a)  $0, \frac{\sqrt{3}}{2}$
- (b)  $-\frac{\sqrt{3}}{2}, \frac{\sqrt{3}}{2}$
- (c)  $-1, \frac{\sqrt{3}}{2}$
- (d) None of these

Answer:

- (b)  $-\frac{\sqrt{3}}{2}, \frac{\sqrt{3}}{2}$

Question 49.

The volume of the tetrahedron whose conterminous edges are  $\hat{j} + \hat{k}, \hat{i} + \hat{k}, \hat{i} + \hat{j}$  is

- (a)  $\frac{1}{6}$  cu. unit
- (b)  $\frac{1}{3}$  cu. unit
- (c)  $\frac{1}{2}$  cu. unit
- (d)  $\frac{2}{3}$  cu. unit

Answer:

- (b)  $\frac{1}{3}$  cu. unit

Question 50.

If the vectors  $2\hat{i} - 3\hat{j}, \hat{i} + \hat{j} - \hat{k}$  and  $3\hat{i} - \hat{k}$  form three concurrent edges of a parallelopiped, then the volume of the parallelopiped is

- (a) 8
- (b) 10
- (c) 4
- (d) 14

Answer:

- (c) 4

Question 51.

The volume of the parallelopiped whose edges are represented by  $-12\hat{i} + \alpha\hat{k}, 3\hat{j} - \hat{k}$  and  $2\hat{i} + \hat{j} - 15\hat{k}$  is 546 cu. units. Then  $\alpha =$

- (a) 3
- (b) 2
- (c) -3
- (d) -2

Answer:

- (c) -3

Question 52.

If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}, \vec{b} = 2\hat{i} - 4\hat{k}, \vec{c} = \hat{i} + \lambda\hat{j} + 6\hat{k}$  are coplanar, then the value of  $\lambda$  is

- (a)  $\frac{5}{2}$  (b)  $\frac{3}{5}$   
(c)  $\frac{7}{3}$  (d) None of these

Answer:

(d) None of these

Question 53.

The value of  $\lambda$ , for which the four points  $2\hat{i} + 3\hat{j} - \hat{k}, \hat{i} + 2\hat{j} + 3\hat{k}, 3\hat{i} + 4\hat{j} - 2\hat{k}, \hat{i} - \lambda\hat{j} + 6\hat{k}$  are coplanar, is

- (a) -2 (b) 8 (c) 6 (d) 0

Answer:

(a) -2

Question 54.

The vectors  $x\hat{i} + (x+1)\hat{j} + (x+2)\hat{k}, (x+3)\hat{i} + (x+4)\hat{j} + (x+5)\hat{k}$  and  $(x+6)\hat{i} + (x+7)\hat{j} + (x+8)\hat{k}$  are coplanar for

- (a) all values of  $x$  (b)  $x < 0$   
(c)  $x \leq 0$  (d) None of these

Answer:

(a) all values of  $x$

Question 55.

If the vectors  $\hat{i} - 2\hat{j} + 3\hat{k}, -2\hat{i} + 3\hat{j} - 4\hat{k}, \lambda\hat{i} - \hat{j} + 2\hat{k}$  are coplanar, then the value of  $\lambda$  is equal to

- (a) 0  
(b) 1  
(c) 2  
(d) 3

Answer:

(a) 0

Question 56.

Find the value of  $\lambda$  if the vectors,  $a = 2\hat{i} - \hat{j} + \hat{k}$ ,  $b = \hat{i} + 2\hat{j} - 3\hat{k}$  and  $c = 3\hat{i} - \lambda\hat{j} + 5\hat{k}$  are coplanar.

- (a) 4
- (b) -2
- (c) -6
- (d) 5

Answer:

- (a) 4

Question 57.

If  $a, b, c$  are unit vectors, then  $|a - b| + |b - c| + |c - a|$  does not exceed

- (a) 4
- (b) 9
- (c) 8
- (d) 6

Answer:

- (b) 9

Question 58.

Find the value of  $\lambda$  so that the vectors  $2\hat{i} - 4\hat{j} + \hat{k}$  and  $4\hat{i} - 8\hat{j} + \lambda\hat{k}$  are perpendicular.

- (a) -15
- (b) 10
- (c) -40
- (d) 20

Answer:

- (c) -40

Question 59.

The dot product of a vector with the vectors  $\hat{i} + \hat{j} - 3\hat{k}$ ,  $\hat{i} + 3\hat{j} - 2\hat{k}$  and  $2\hat{i} + \hat{j} + 4\hat{k}$  are 0, 5 and 8 respectively. Find the vector.

- (a)  $\hat{i} + 2\hat{j} + \hat{k}$
- (b)  $-\hat{i} + 3\hat{j} - 2\hat{k}$
- (c)  $\hat{i} + 2\hat{j} + 3\hat{k}$
- (d)  $\hat{i} - 3\hat{j} - 3\hat{k}$

Answer:

- (a)  $\hat{i} + 2\hat{j} + \hat{k}$

Question 60.

If  $a, b, c$  are three mutually perpendicular vectors of equal magnitude, find the angle between  $a$  and  $a + b + c$ .

- (a)  $\cos^{-1}(1/\sqrt{3})$

(b)  $\cos^{-1}(1/2\sqrt{2})$

(c)  $\cos^{-1}(1/3\sqrt{3})$

(d)  $\cos^{-1}(1/2\sqrt{3})$

Answer:

(a)  $\cos^{-1}(1/\sqrt{3})$